

Calculations on motion of objects in a lift

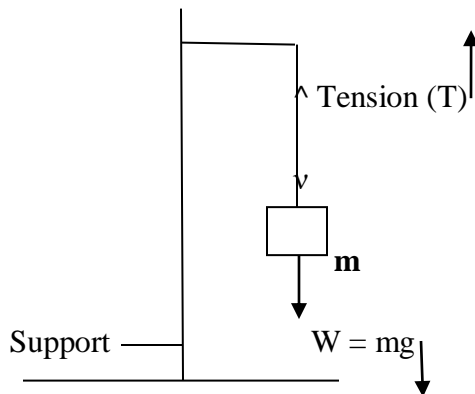
- 1) A man of mass **65kg** is accelerated upwards from the ground floor to the fifth floor in a lift at a rate of **2ms^{-2}** .
- Draw a diagram to show the forces acting in the motion system.
 - Indicate the direction of motion, with acceleration of the lift.
 - Calculate:
 - The resultant force producing the acceleration in (b) above.
 - The value of reaction force, **R** on the man in the lift.
 - Compare:
 - The value of reaction force, **R** that the man feels as his weight to the value of his actual (normal) weight, **W**.
 - What do you conclude from your comparison above in terms of his weight?*
- 2) A girl of mass **80kg** stands on a weighing scale on the floor of the lift. Calculate:
- The resultant force on the girl
 - The reaction in Newtons on the weighing scale if the lift moves:
 - Upwards with an acceleration of **2ms^{-2}** .
 - Down wards with an acceleration of **2ms^{-2}**
 - Upwards with a constant velocity of **6ms^{-1}** .
 - Compare your answers in (b) above and make a conclusion about what happens to the weight of a person in each case of motion in a lift.

TENSION IN A STRING

Tension is the force which pulls the ends of an object apart when it is applied. It's a stretching force.

Tension acts towards a fixed point of support when the body is at rest or moving at a constant velocity.

Illustration: consider a mass, m suspended on a support using inextensible string.



The mass, m is suspended on a support using an inextensible string. The force of gravity acts on the mass downwards. The tension force results in the string since it is tied to a rigid support. Two forces act on the mass. i.e. its weight, $\mathbf{W} = \mathbf{mg}$ and the tension force, \mathbf{T} (in the string). When the mass is at rest, its acceleration $\mathbf{a} = \mathbf{0} \text{ ms}^{-2}$.

Now, using Newton's second law of motion,

$$\mathbf{T} - \mathbf{mg} = \mathbf{ma}$$

$$\mathbf{T} = \mathbf{m} \times \mathbf{a} + \mathbf{mg}$$

$$\mathbf{T} = \mathbf{m} (\mathbf{a} + \mathbf{g}), \text{ but } \mathbf{a} = \mathbf{0}$$

$$\mathbf{T} = \mathbf{m} (\mathbf{0} + \mathbf{g}) = \mathbf{mg}$$

$$\mathbf{T} = \mathbf{mg}$$

If the tension force causes the object to accelerate upwards with a ms^{-2} , then;

$$\mathbf{T - mg = ma}$$
 (resultant force)

$$\mathbf{T = ma + mg}$$

OR $\mathbf{T = m(a + g)}$

So, in this case the tension in the string is greater than when the mass is at rest.

If the object accelerates downwards with acceleration, $\mathbf{a \text{ ms}^{-2}}$ but still attached to the string, then;

$$\mathbf{mg - T = ma}$$
 (Newton's 2nd law of motion)

$$\mathbf{T = mg - ma}$$
 (reduction in Tension force)

Or $\mathbf{T = m(g - a)}$

If the mass moves with a steady/constant speed, i.e. $\mathbf{a = 0 \text{ ms}^{-2}}$, then,

$$\mathbf{T - mg = ma}$$
 (Newton's 2nd law of motion)

$$\mathbf{T - mg = 0}$$

$$\mathbf{T = mg}$$

Calculations involving Tension force (T)

1) A bail of cotton of mass **100g** is pulled upwards by a **5N** force.

Calculate;

- a) Weight of the bail
- b) Resultant force on the bail
- c) The upward acceleration

- 2) A crane lifter raises a container of mass **400kg** suspended on inextensible string.
- Draw a diagram and indicate the forces acting on the mass of the container.
 - If the force in the string is 4800. Find the acceleration of the mass as it rises.
 - Calculate the value of force in the string which makes the mass of the container to move with a constant speed.
- 3) A spring balance carrying a mass of 4kg is suspended from a ceiling of a lift. Calculate the reading on the spring balance when the;
- Lift is ascending with an acceleration of 0.4ms^{-2}
 - Lift is descending with an acceleration of 0.4ms^{-2}
 - Lift is ascending with uniform velocity.

END